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(Ex 1) (3 pt) Establish the convergence of the series  $\sum_{n=1}^{\infty} \cos\left(\frac{\pi}{2}(2n+1)\right)$  using the sequence of partial sums  $(S_n)$ .

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(Ex 2) (2 pt) Apply the necessary condition for convergence to the series  $\sum_{n=1}^{\infty} \frac{1}{n^2}$ .

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(Ex 3a) (2 pts) Establish the convergence of the series  $\sum_{n=1}^{\infty} \sin^n\left(\frac{\pi n+1}{4n+1}\right)$  using an appropriate test.

(Ex 3b) (1 pt) Write the definition of the test you used.

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(Ex 4) (3 pts) Establish, whether the series  $\sum_{n=1}^{\infty} (-1)^n \frac{n^2}{n^4+2}$  is absolutely convergent, conditionally convergent or divergent.

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(Ex 5) (2 pts) Show that the limit  $\lim_{(x,y) \rightarrow (0,0)} \frac{5x^2y^2}{x^4+3y^4}$  doesn't exist. Use any method you like.

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(Ex 6) (4 pts) Find all extremes and saddle points of the function  $f(x, y) = x^3 + 8y^3 - 6xy + 5$ .

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Ex 7) (2 pts) Check if  $f(x, y) = \ln(x^2 + y^2)$  is the answer to an equation  $f_x + f_y = \frac{(2yx+y^2)'_y}{x^2+y^2}$ .

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(Ex 8) (1 pt) Describe the procedure of changing Cartesian coordinates  $(x, y)$  into polar coordinates. Draw a graph.

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(Ex 9) (2 pts) **Bonus exercise:** Find the approximated value and both errors for  $\ln(1.01) \cdot \frac{1}{2.01} \cdot (4.95)^2$  if you know that  $V_c = 0.121298$ .